



Cambridge International AS & A Level

CANDIDATE
NAME

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FURTHER MATHEMATICS

9231/42

Paper 4 Further Probability & Statistics

October/November 2020

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages. Blank pages are indicated.

- 2 A large school is holding an essay competition and each student has submitted an essay. To ensure fairness, each essay is given a mark out of 100 by two different judges. The marks awarded to the essays submitted by a random sample of 12 students are shown in the following table.

Student	A	B	C	D	E	F	G	H	I	J	K	L
Judge 1	62	74	52	48	68	55	56	64	37	70	81	59
Judge 2	65	70	47	49	76	74	67	54	50	77	72	75

- (a) One of the students claims that Judge 2 is awarding higher marks than Judge 1.

Carry out a Wilcoxon matched-pairs signed-rank test at the 5% significance level to test whether the data supports the student's claim. [7]

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It is discovered later that the marks awarded to student A have been entered incorrectly. In fact, Judge 1 awarded 65 marks and Judge 2 awarded 62 marks.

- (b) By considering how this change affects the test statistic, explain why the conclusion of the test carried out in part (a) remains the same. [2]

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(c) Find $\text{Var}(\sqrt{\bar{X}})$. [2]

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(d) The random variable Y is defined by $Y = X^3$. Find the probability density function of Y . [3]

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6 Nassa is researching the lengths of a particular type of snake in two countries, *A* and *B*.

- (a) He takes a random sample of 10 snakes of this type from country *A* and measures the length, x m, of each snake. He then calculates a 90% confidence interval for the population mean length, μ m, for snakes of this type, assuming that snake lengths have a normal distribution. This confidence interval is $3.36 \leq \mu \leq 4.22$.

Find the sample mean and an unbiased estimate for the population variance. [4]

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- (b) Nassa also measures the lengths, y m, of a random sample of 8 snakes of this type taken from country *B*. His results are summarised as follows.

$$\sum y = 27.86 \quad \sum y^2 = 98.02$$

Nassa claims that the mean length of snakes of this type in country *B* is less than the mean length of snakes of this type in country *A*. Nassa assumes that his sample from country *B* also comes from a normal distribution, with the same variance as the distribution from country *A*.

Test at the 10% significance level whether there is evidence to support Nassa’s claim. [8]

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